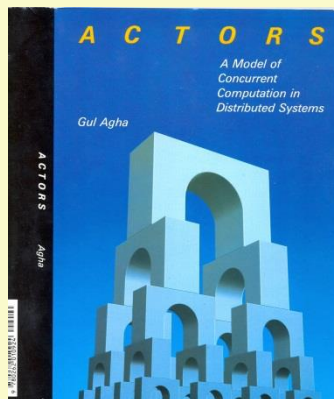


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# Abstractions, Semantic Models and Analysis Tools for Concurrent Systems: Progress and Open Problems

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## *Motivation*

# INTERNET OF THINGS TO ENABLE SMART INFRASTRUCTURE

# The Aging Civil Infrastructure

America's **\$20 trillion+** investment in civil infrastructure is in dire shape, and will continue to deteriorate if we fail to act.



Bridge	C
Roads	D-
Rail	C-
Dams	D
Levees	D-
Energy	D+
Aviation	D
Waste Water	D-
Solid Waste	D+
Water	D-

American Society of Civil Engineers report card grades

**Continuous monitoring** and precision targeting of maintenance can improve safety and save billions of dollars for infrastructure owners.

# Sensor Clouds for Smart Infrastructure

- Smart infrastructure can improve safety, facilitate smart transportation systems.

**Infrastructure is aging.  
Estimated 70,000 structurally deficient bridges in US.**

- Monitor infrastructure, pinpoint deficiencies.
- Control: dampen vibrations to limit damage
- *Scalable cyberphysical systems required.*

# Keeping Tabs on the Infrastructure



“... one highly **intelligent bridge** knows what to do when trouble arises: send an e-mail.”

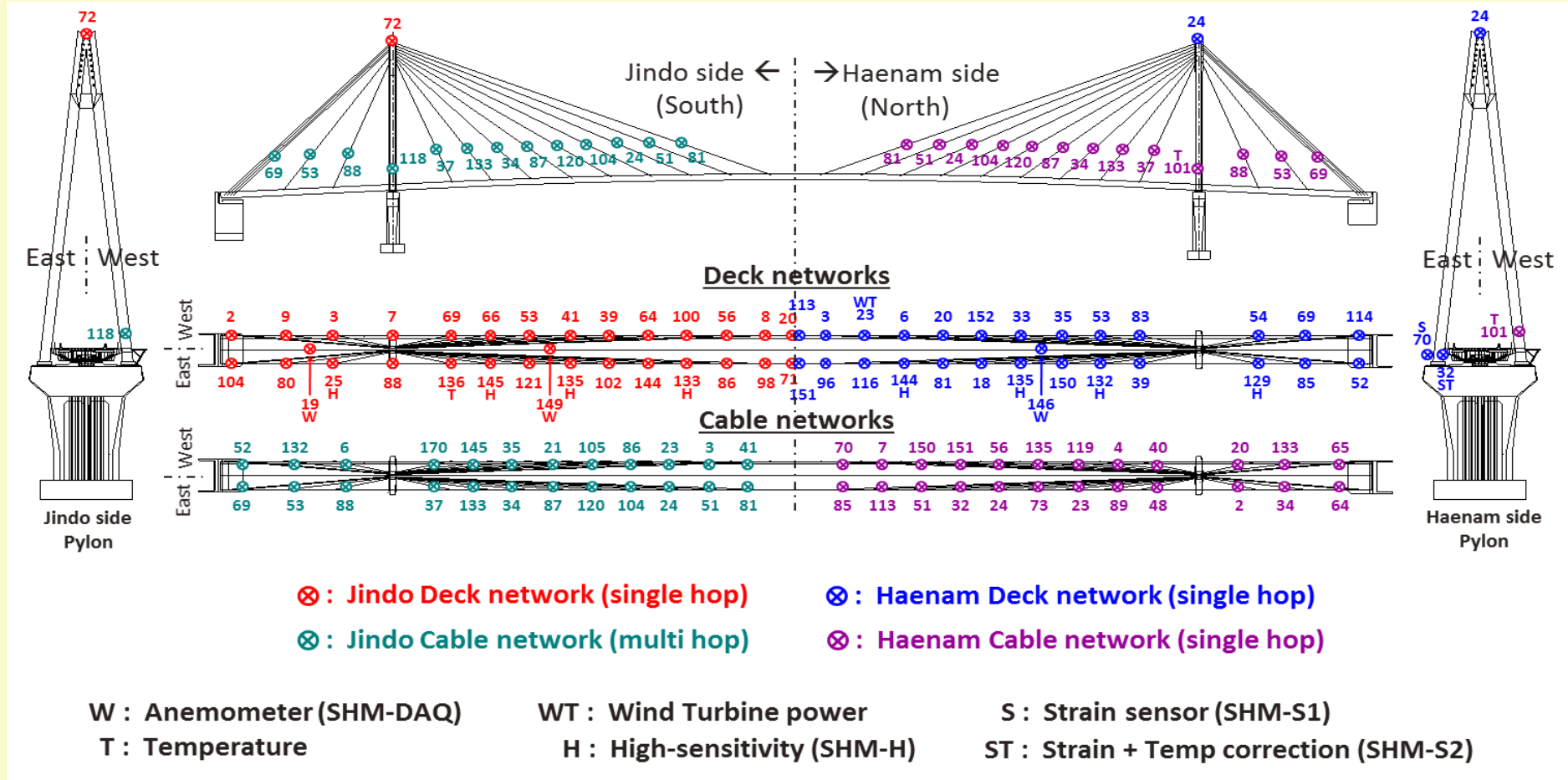
**The New York Times**

*“A small army of electronic sentinels... monitor the bridge’s structural health. (As of last week, the bridge said it was just fine.)”*

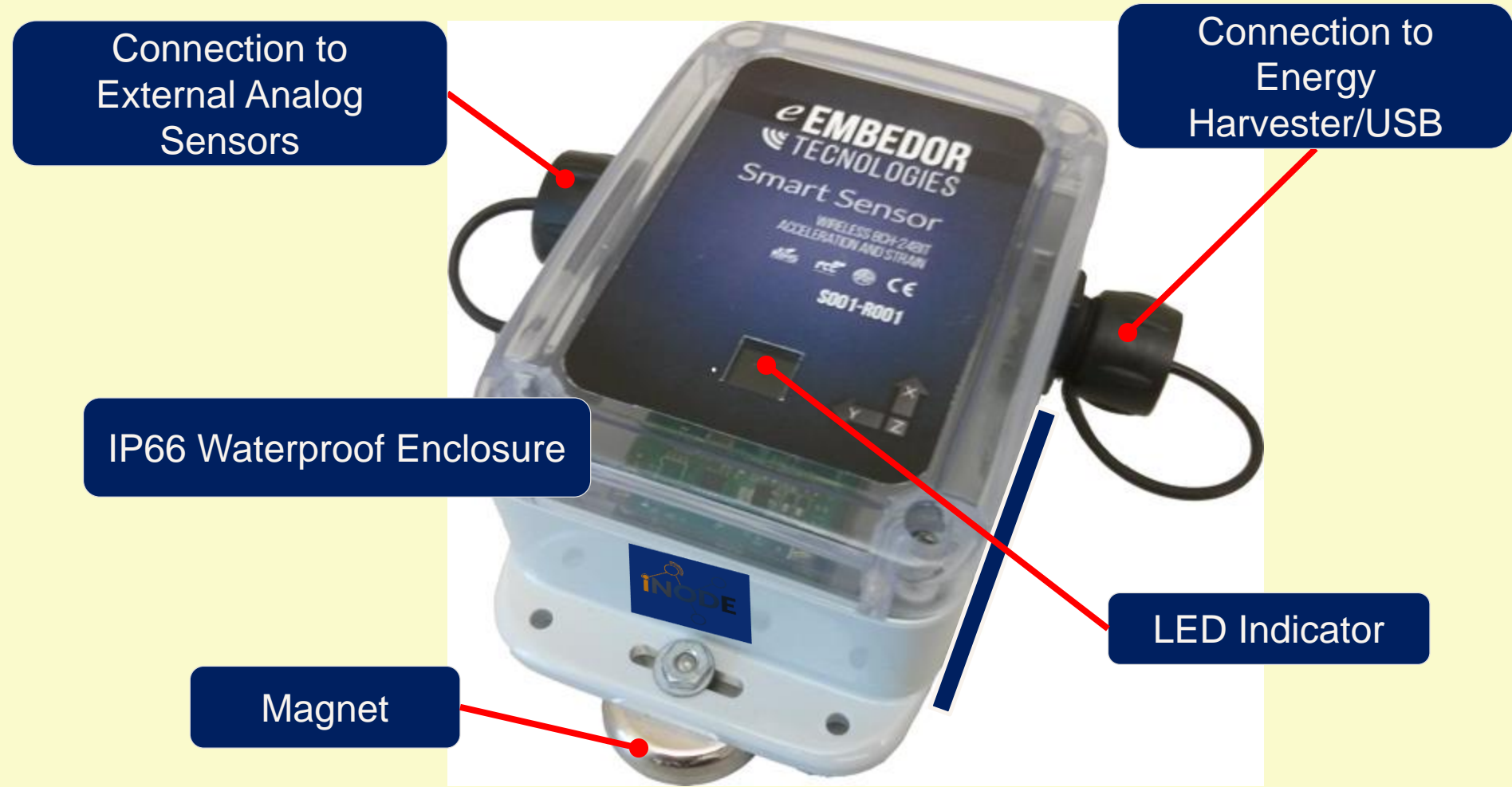


*Illinois Structural Health Monitoring Project*  
**See: <http://shm.cs.illinois.edu>**

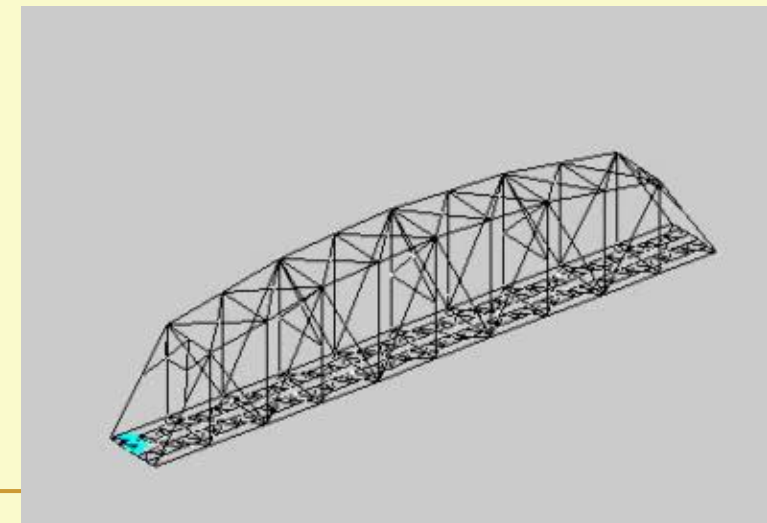
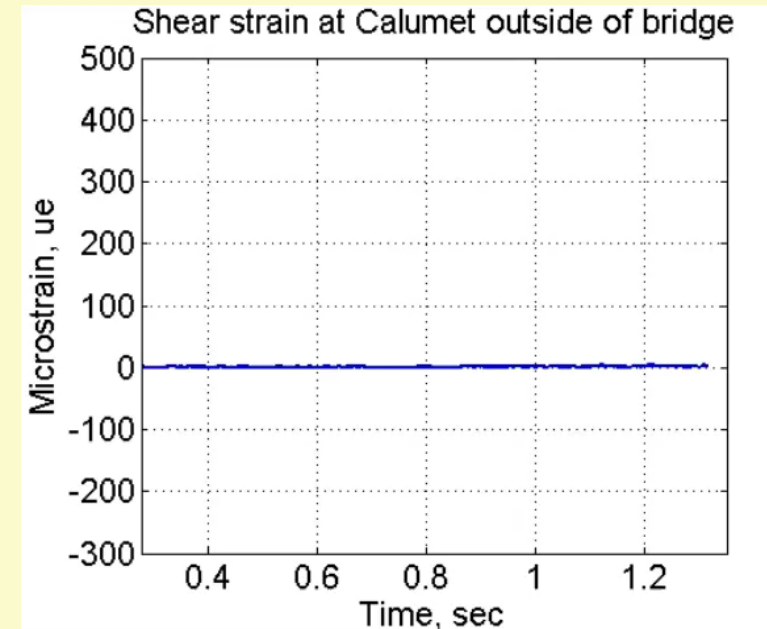
# Dense Sensor Clouds for Smart Structures



# *xnode*: Environmentally Hardened Enclosure

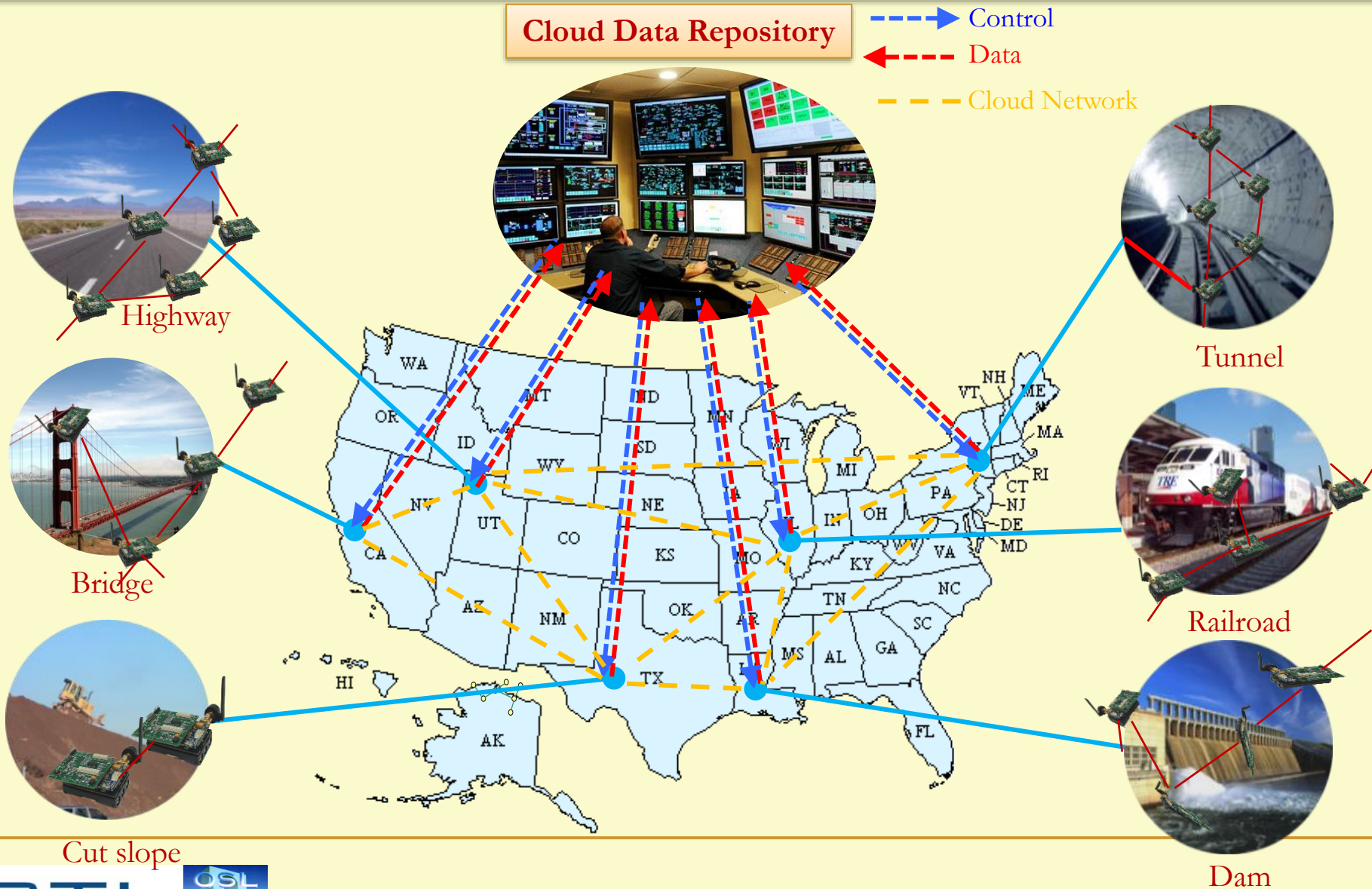






A calibrated model and strategically placed smart sensors allow for the force in all structural members to be determined with high accuracy and *remaining service life* to be estimated. Checkout the video at: <http://embedortech.com>

# Example: National Smart Structures Grid





# MODELS OF CONCURRENCY



# Models of Concurrency

- Petri Nets
- Process Algebras
- Actors

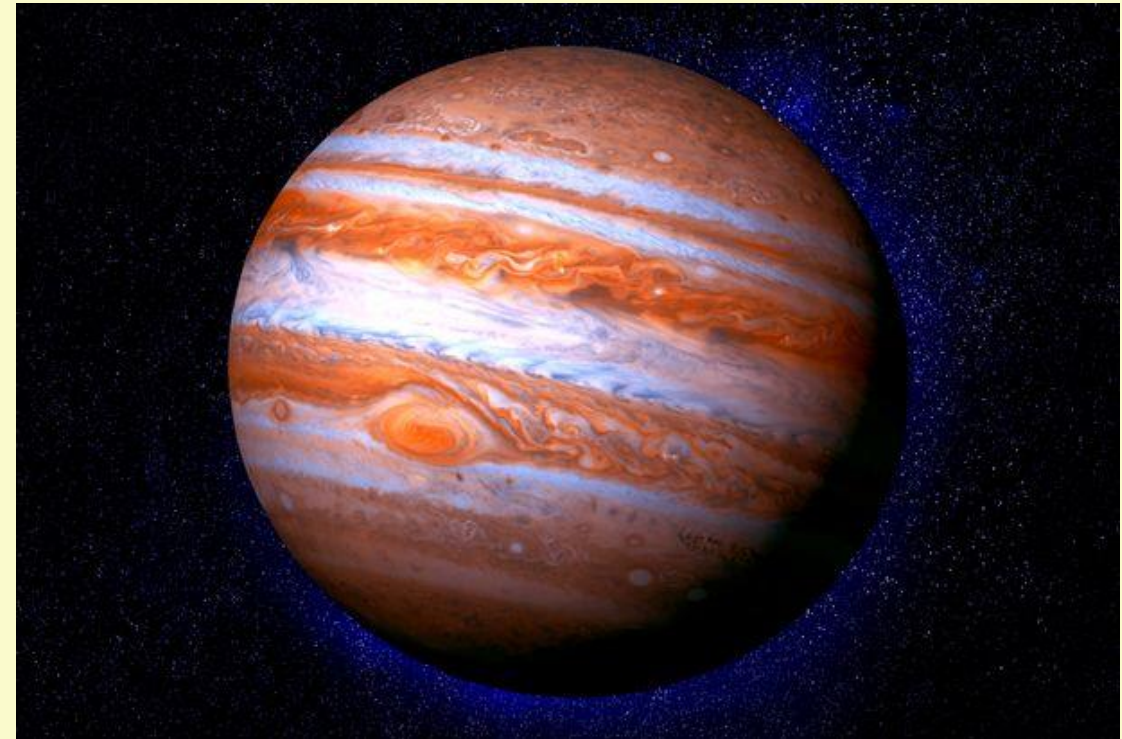


# Programming *Scalable* Applications

- Efficiency
- Distribution
- Concurrency
- Scalability
- Stability and Robustness

# Scalable Applications

- Martian Rover (1990s)
- Twitter's message queuing
- LiftWeb Framework (Scala for web applications)
- Image processing in MS Visual Studio 2010
- Vendatta game engine (Erlang)
- Facebook Chat System (Erlang)
- LinkedIn
- Microsoft Orleans: used by >343 industries, platform for all of Halo 4 cloud services



***33 to 49 minutes for radio waves to travel from Jupiter to Earth***

# Concurrency



“When people read about Scala, it's almost always in the context of concurrency. Concurrency can be solved by a good programmer in many languages, but it's a tough problem to solve. Scala has an *Actor library* that is commonly used *to solve concurrency problems, and it makes that problem a lot easier to solve.*”

--Alex Payne, “*How and Why Twitter Uses Scala*”

[http://blog.redfin.com/devblog/2010/05/how\\_and\\_why\\_twitter\\_uses\\_scala.html](http://blog.redfin.com/devblog/2010/05/how_and_why_twitter_uses_scala.html)

(emphasis added)

# Stability and Scalability

“..the *actor model has worked really well* for us, and we wouldn't have been able to pull that off in C++ or Java. Several of us are big fans of Python and I personally like Haskell for a lot of tasks, but the bottom line is that, while those languages are great general purpose languages, none of them were designed with the actor model at heart.”

--Facebook Engineering

<https://www.facebook.com/notes/facebook-engineering/chat-stability-and-scalability/51412338919>



# Actor Languages and Frameworks

- Erlang
- E
- Axum
- Stackless Python
- Theron (C++)
- RevActor (Ruby)
- Dart
- Asynchronous Agents Library
- Scala Actors/Akka
- ActorFoundry
- SALSA
- Kilim
- Jetlang
- Actor's Guild
- Clojure
- ... a growing list

# Characteristics of the Actor Model

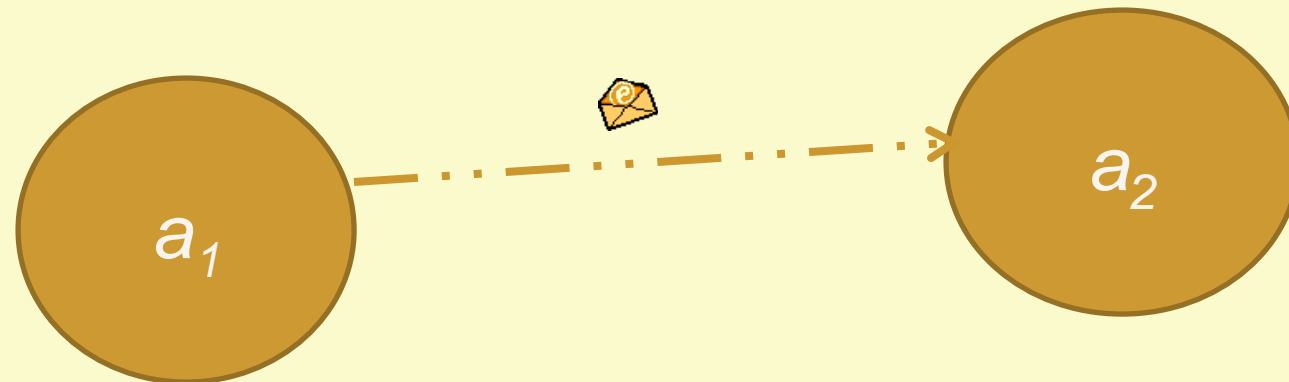
Computation broken into autonomous, concurrent agents called *actors*:

- Actors do not share state
  - Analogous to animals in natural systems.
- Each actor operates asynchronously
  - The rate at which an actor operates may vary.
  - An actor is like a *virtual processor*.
- An actor may interact with other actors.

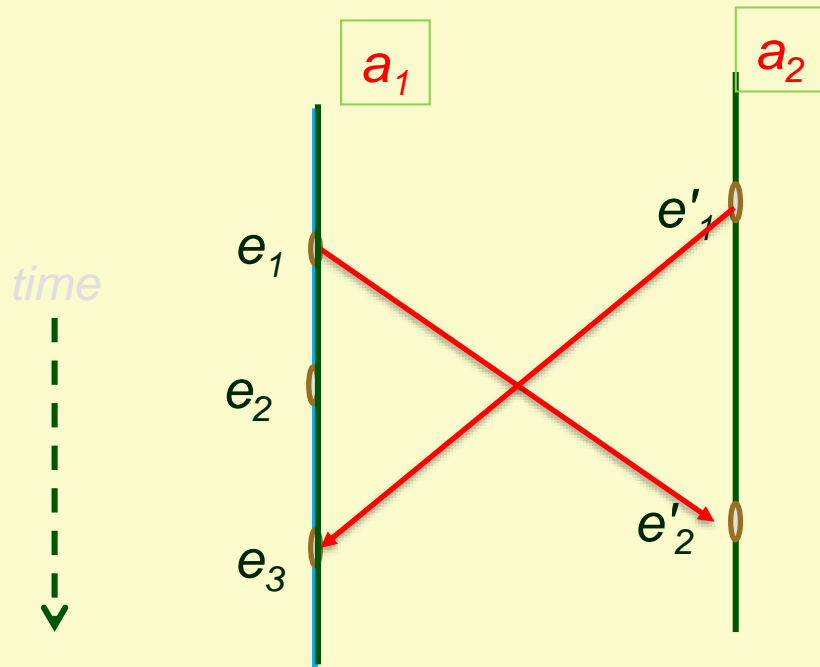
[Actors: A Model of Concurrent Computation in Distributed Systems," Gul Agha. MIT Press, 1986.]

# Message-Passing

- There is no action at a distance
- An actor  $a_1$  can only affect  $a_2$  by sending it a message.
- Messages are asynchronous



# Distribution and Parallelism



- Each actor represents a point in a virtual space.
- Events at an actor are ordered linearly.
- Events may change the state of an actor
- An event on one actor may activate an event on another by sending a message (causal order).
- Transitive closure results in a partial order

# Fairness

- Each actor makes progress if it can:
  - *If multiple actors execute on a single processor, each actor is scheduled.*
- Every messages is eventually delivered if it can be:
  - *When an actor is idle and has a pending message, it processes that message.*
  - *Multiple pending messages are processed in an order so none is permanently ignored by the target actor.*

# Actor Names

- The *name (mail address)* of each actor is unique and cannot be guessed.
- An actor must know the *name (mail address)* of the target actor to send it a message
  - Called the *locality property* of actors.
- Locality property provides a built in *capability architecture* for security.

# Actor Topology

- If an actor  $a_1$  knows the address of another actor  $a_2$ ,  $a_1$  may communicate the name of an  $a_2$  in a message.
  - The interconnection topology of actors is dynamic.
- Supports mobility and reconfiguration of actors.

# Actor Creation

New actors may be created:

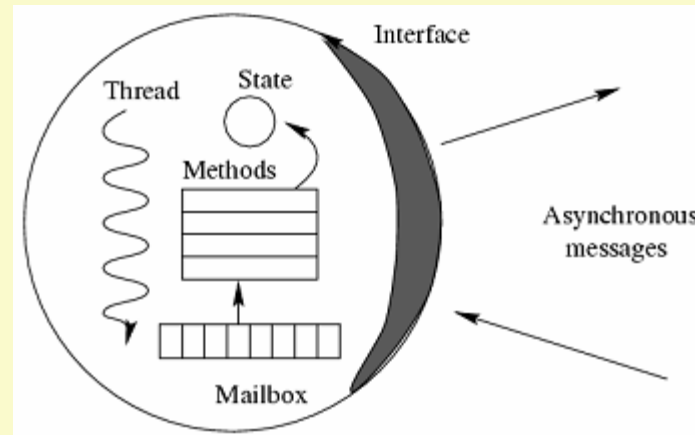
- Increases the available concurrency in a computation.
- Facilitates dynamic parallelism for load balancing.
- Enables mechanisms for fault-tolerance.



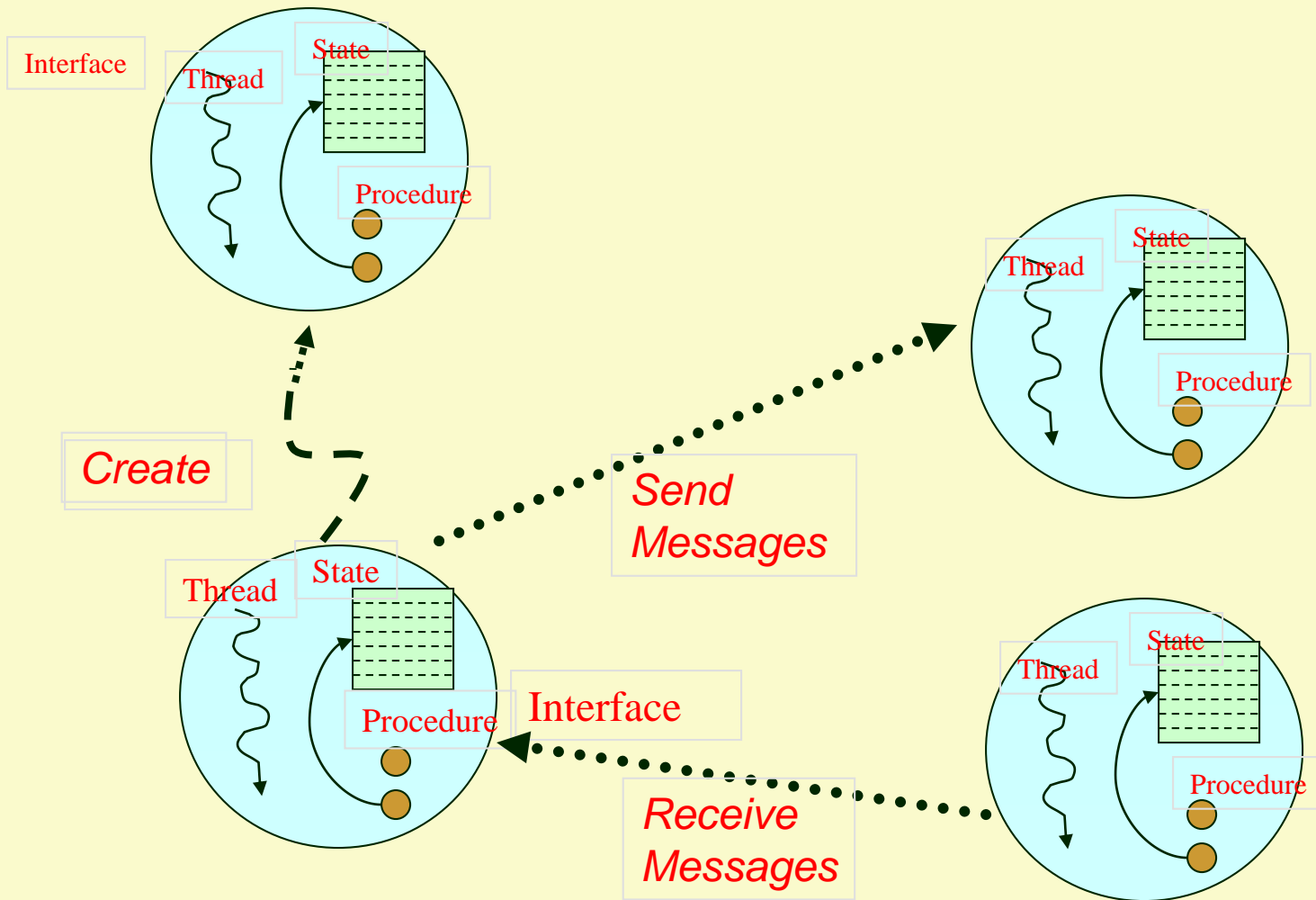
# Actor anatomy: Actors and Threads

Actors = encapsulated state + behavior +  
independent control + mailbox

Object



# The Actor Model: Runtime Support



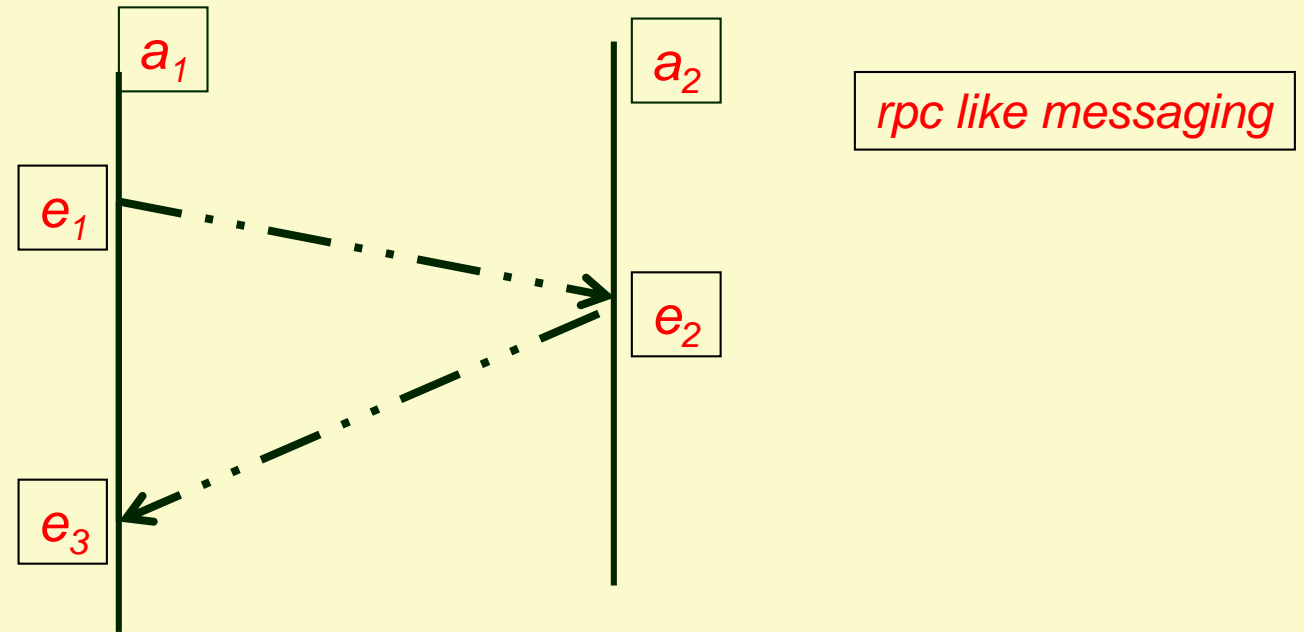
# Defining an actor language

Start with a sequential object-based language or framework, add concurrency to objects, operators for:

- actor creation
  - `create(class, params)`
  - *Locally or at remote nodes*
- message sending
  - `send(actor, method, params)`
- state change
  - ready to process next message

# Message Patterns

- More complex message patterns may be defined in terms of asynchronous messages:



**Actor Event Diagrams**

# Actor Encapsulation: State Isolation

- Recall: *no shared state* between actors
- ‘Access’ another actor’s state *only* by sending it a message and requesting it:
  - Messages have send-by-value semantics
  - Implementation may be relaxed on shared memory platforms, if “safe”

# Location Transparent Naming

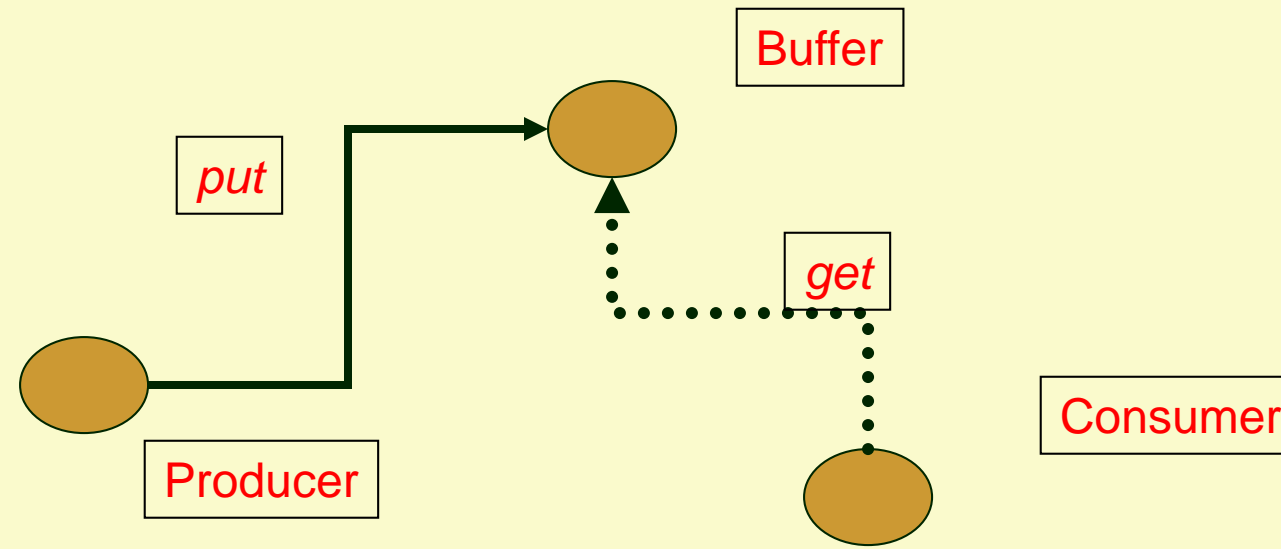
- Enables *automatic* load-balancing and fault-tolerance mechanisms
  - Run-time can exploit resources available on cluster, grid or scalable multicores (distributed memory)
- Uniform model for multicore and distributed programming



# Synchronization and Coordination

- Essential for correct functioning of actor systems
- A source of complexity in concurrent programs

# Synchronizing in a Concurrent World



- The interface of an actor may be dynamic:
  - ❑ Cannot get from an empty buffer
  - ❑ Cannot put into a full buffer



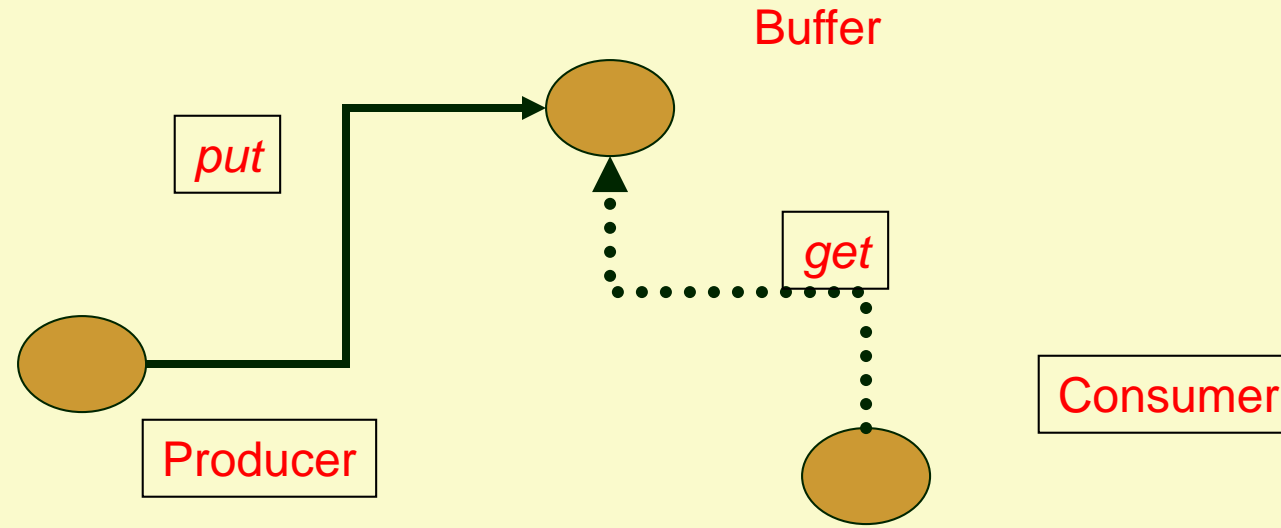
# Separation of Concerns

- Abstract Data Types:
  - Enable separation of *interface (what)* from the *representation (how)*.
- Actors:
  - *When* actions happen is underspecified (*asynchrony*).
  - Recipient may not be ready to process a message when it arrives – *synchronization constraints (when)*.
  - Separate specification of *when* from *how* to facilitate modularity in code.

# Local Synchronization Constraints

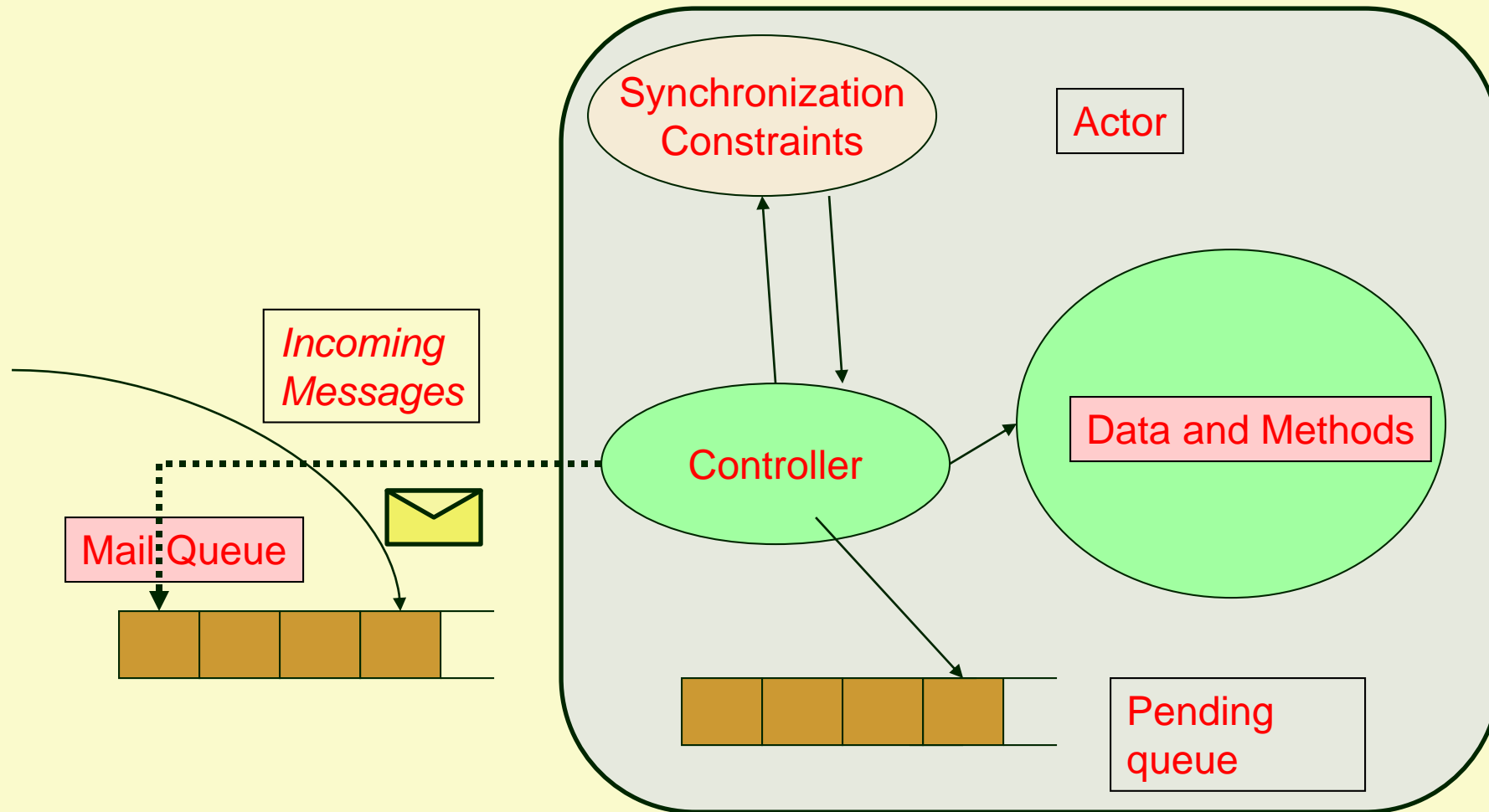
- Constrain the “local” order of processing messages
  - Delay or reject out of order messages
  - Function of local state and message contents
- These have *delay* semantics i.e. disabled messages are buffered
- Implementations: Disabling constraints in AF, Pattern matching in Erlang, Scala

# Expressing Local Synchronization Constraints (Abstractly)



- Per actor logical rules which determine the legality of invocations:
  - disable get when empty? (buffer)

# Implementation of Local Synchronization Constraints



# Scalable Reasoning Tools

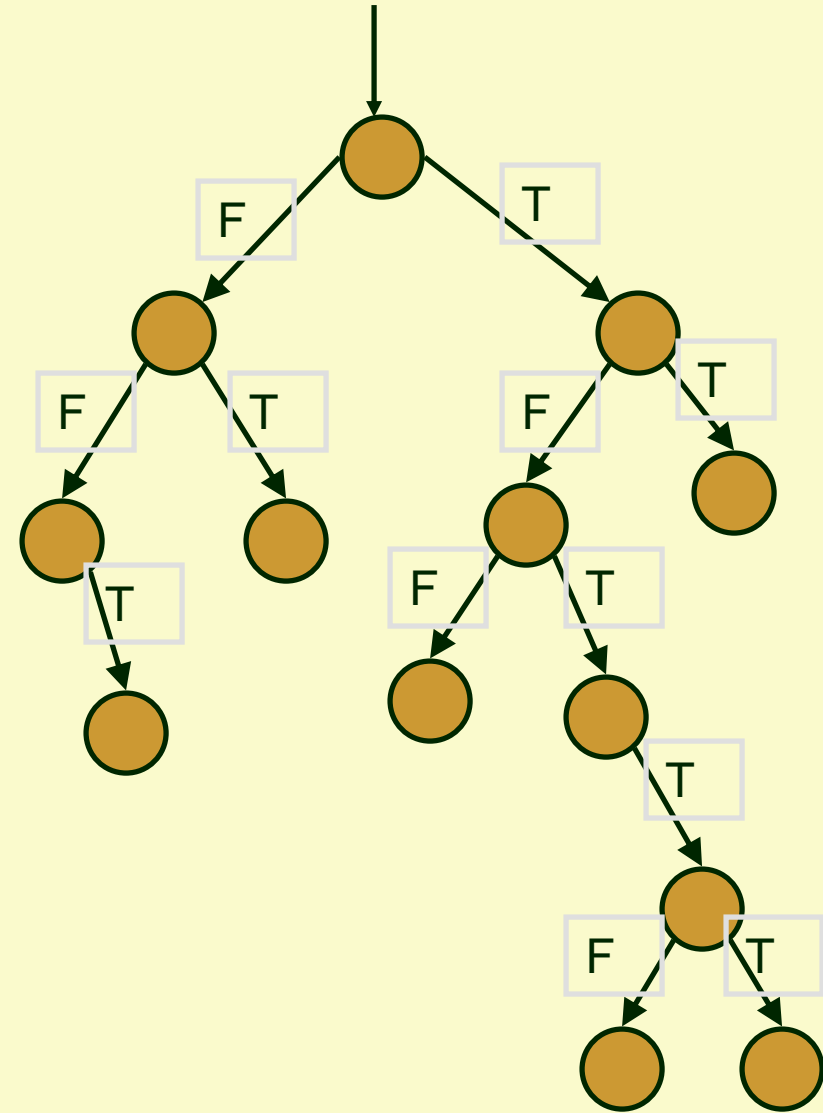
- Computational Learning for Verification
- Concolic Testing and its variants
- Runtime verification (Monitoring)
- Inferring interfaces: session types, concurrency structure
- Computational learning for verification (won't discuss today)

## Quantitative Tools:

- Statistical Model Checking
- Euclidean Model Checking

# Execution Paths of a Program

- Can be seen as a **binary tree** with possibly infinite depth
  - **Computation tree**
- Each **node** represents the execution of a “**if then else**” statement
- Each **edge** represents the execution of a sequence of non-conditional statements
- Each path in the tree represents an equivalence class of inputs.
- *What about loops?*
  - *Unroll to finite depth.*



# What is Testing?

- Execute the program and observe how it behaves under different scenarios:
  - Vary the inputs.
  - In concurrent programs: vary the schedules.

# Goal

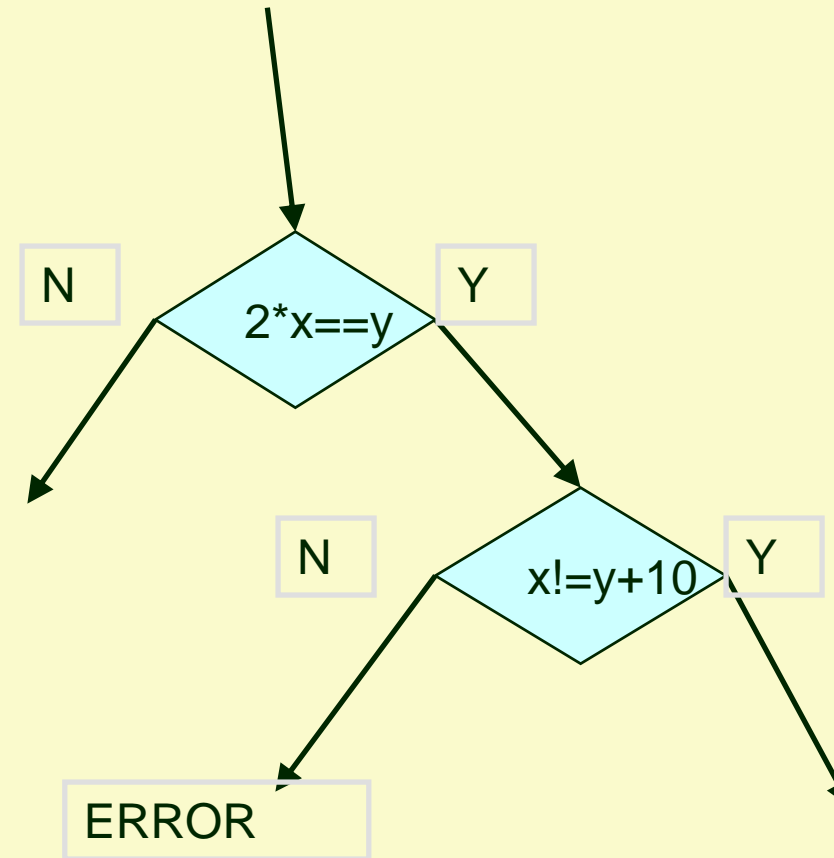
- Automated Scalable Unit Testing of real-world sequential programs
  - Generate test inputs
  - Execute unit under test on generated test inputs
    - so that all reachable statements are executed
  - Any assertion violation gets caught





# Example of Computation Tree

```
void test_me(int x, int y) {  
    if(2*x==y){  
        if(x != y+10){  
            printf("I am fine here");  
        } else {  
            printf("I should not reach here");  
            ERROR;  
        }  
    }  
}
```



# Random Testing

- generate random inputs
- execute the program on generated inputs
- Probability of reaching an error can be astronomically less

```
test_me(int x){  
    if(x==94389){  
        ERROR;  
    }  
}
```

Probability of hitting **ERROR** =  
 $1/2^{32}$

# Symbolic Execution

- use symbolic values for input variables
- execute the program symbolically on symbolic input values
- collect symbolic path constraints
- use theorem prover to check if a branch can be taken

```
test_me(int x){  
    if (x==94389){  
        ERROR;  
    }  
}
```

# Symbolic Execution

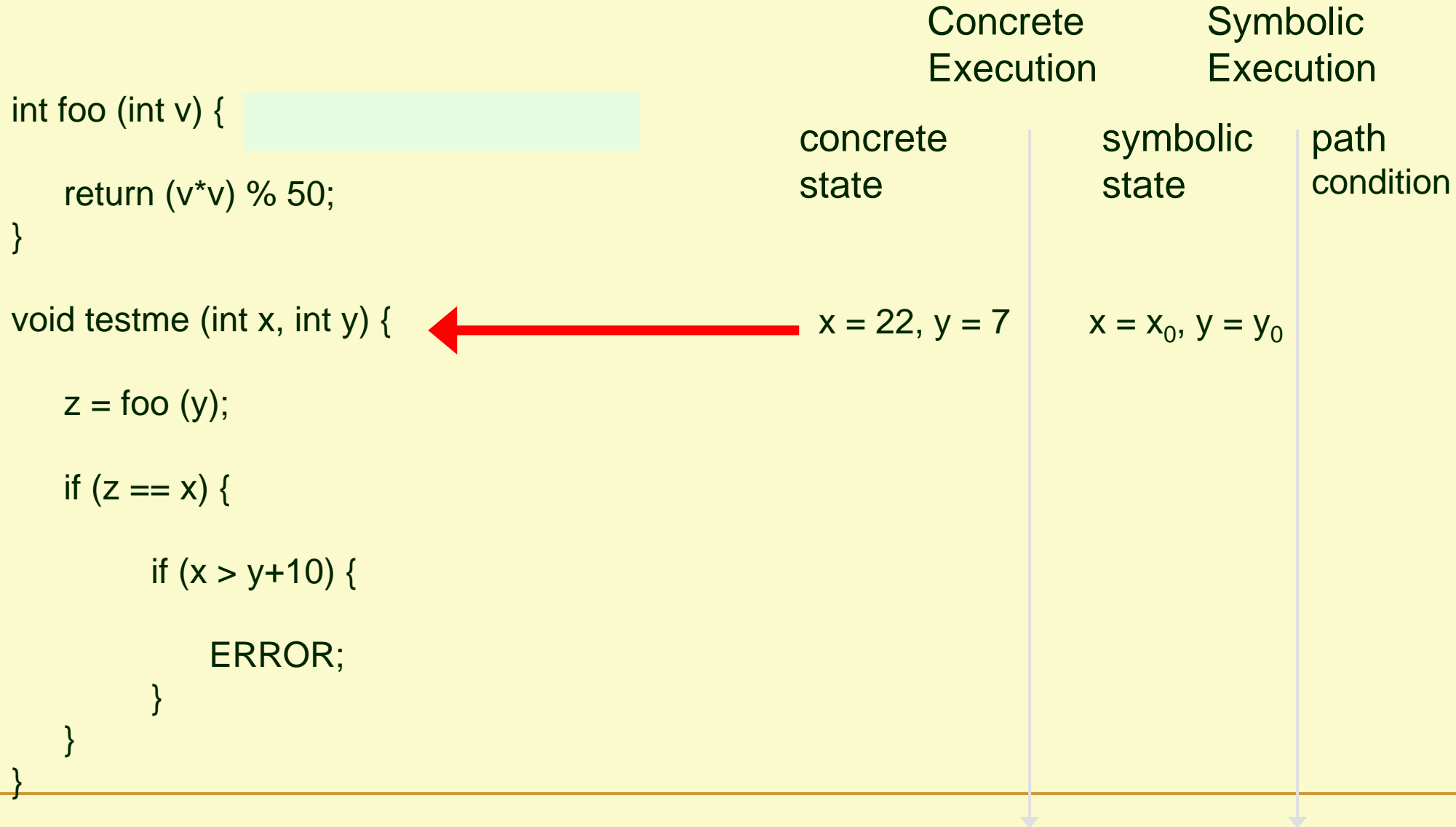
- What if we can solve the constraint?
- Symbolic execution will say both branches are reachable:  
**False positive**
- Does not scale for large programs

```
test_me(int x){  
    if((x%10)*4!=17){  
        ERROR;  
    } else {  
        ERROR;  
    }  
}
```

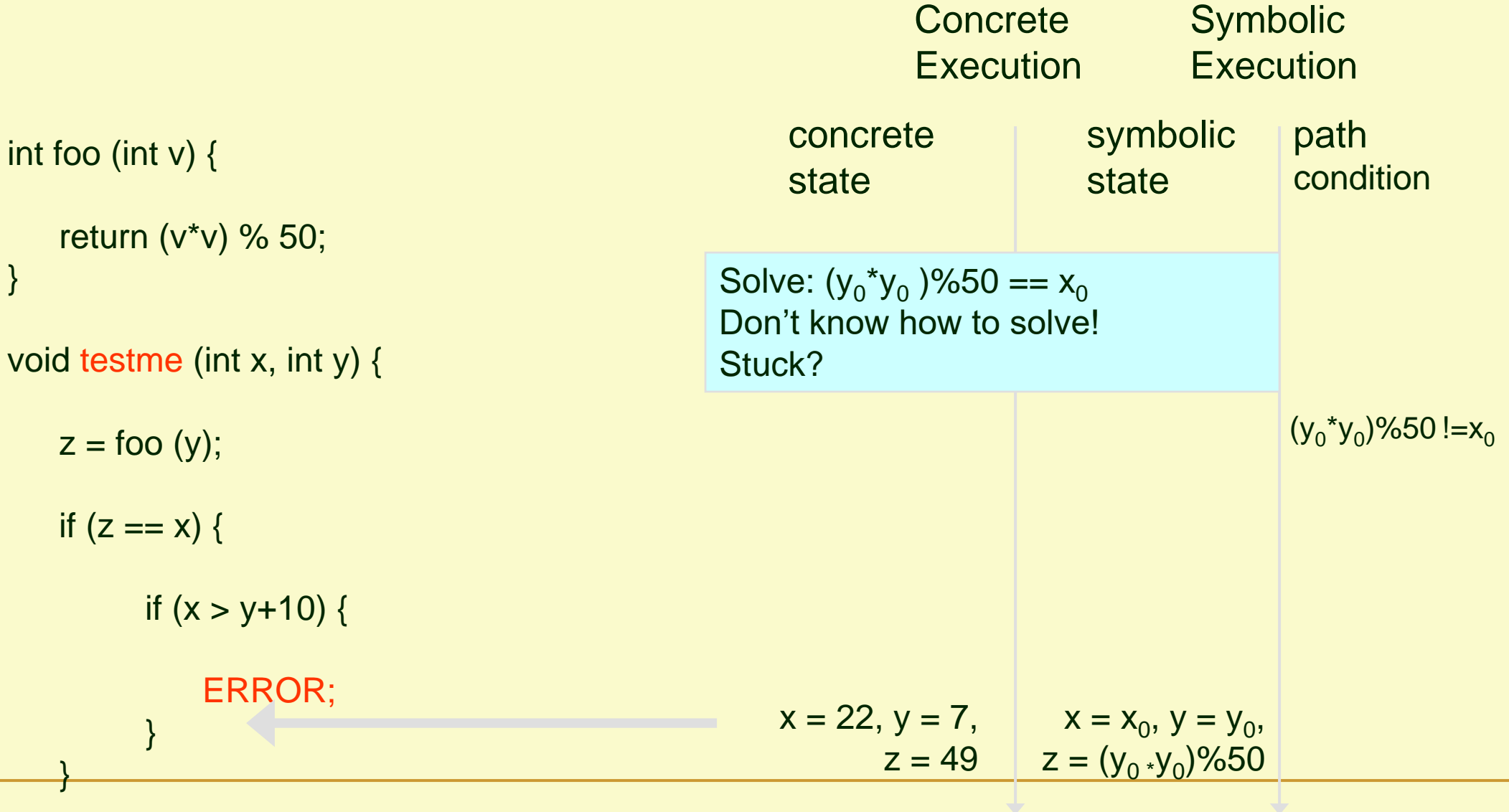
# Approach

- Combine concrete and symbolic execution for unit testing
  - **Concrete** + **Symbolic** = **Concolic**
- In a nutshell
  - Use concrete execution over a concrete input to guide symbolic execution
  - Concrete execution helps Symbolic execution to simplify complex and unmanageable symbolic expressions
    - by replacing symbolic values by concrete values
- **Achieves Scalability**
  - Higher branch coverage than random testing
  - No false positives or scalability issue like in symbolic execution based testing

# Example: Simultaneous Concrete and Symbolic Execution

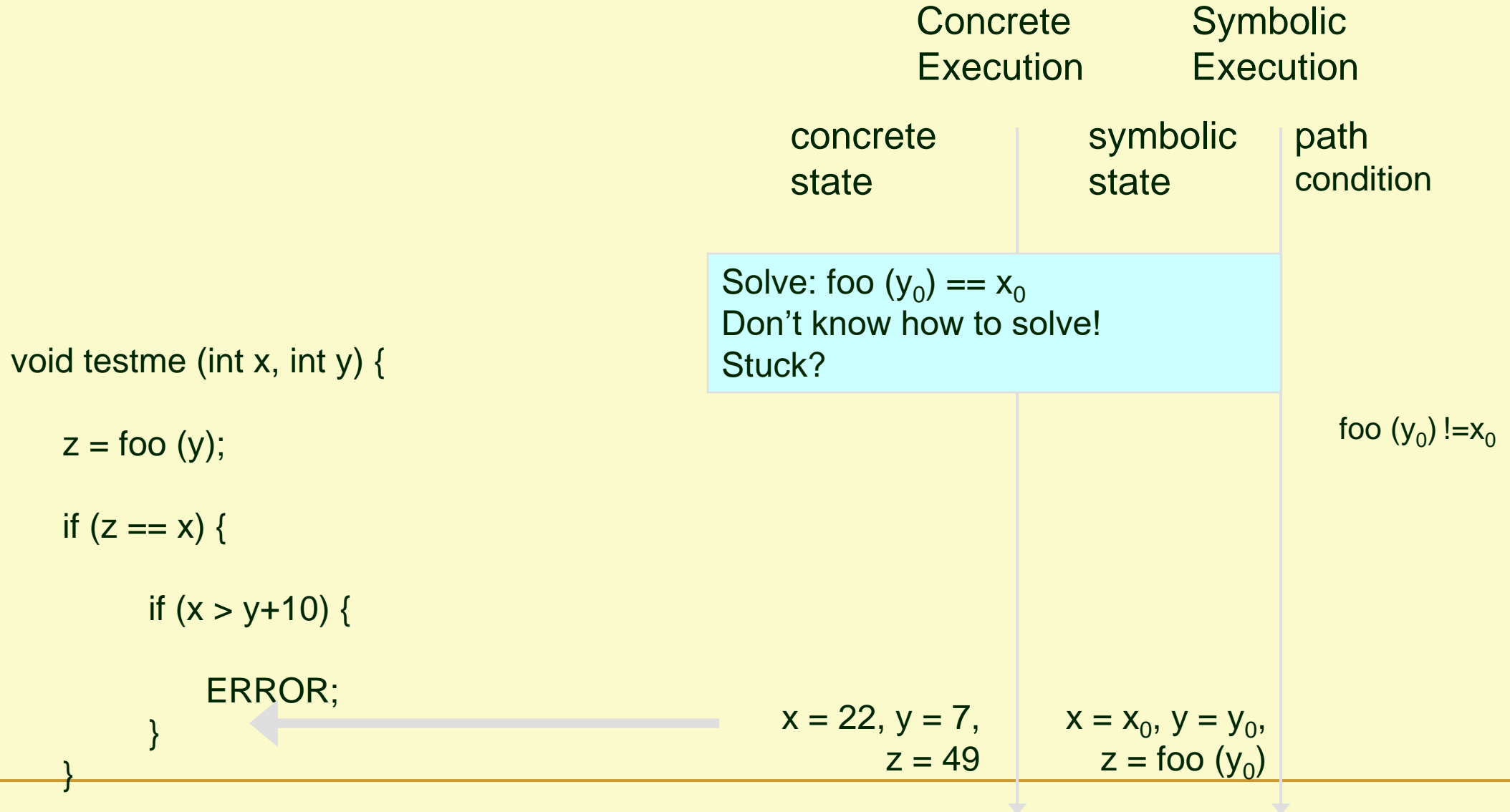


# Example : Simultaneous Concrete and Symbolic Execution

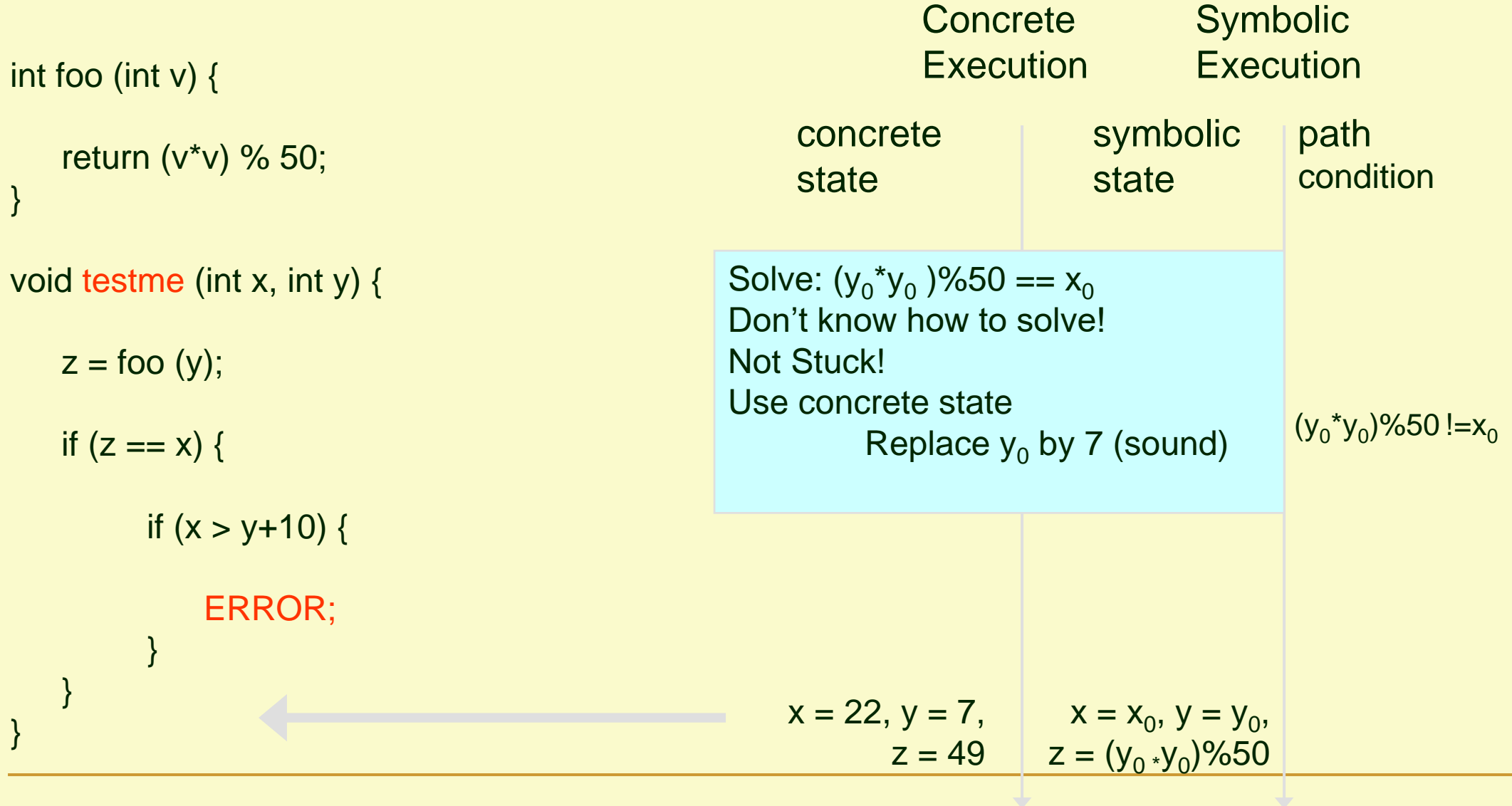




# Example : Simultaneous Concrete and Symbolic Execution



# Example : Simultaneous Concrete and Symbolic Execution



# Example : Simultaneous Concrete and Symbolic Execution

Concrete Execution

Symbolic Execution

```
int foo (int v) {
    return (v*v) % 50;
}

void testme (int x, int y) {
    z = foo (y);
    if (z == x) {
        if (x > y+10) {
            ERROR;
        }
    }
}
```

concrete state

symbolic state

path condition

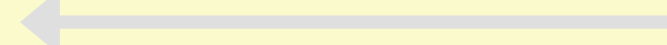
Solve:  $49 == x_0$   
Solution :  $x_0 = 49, y_0 = 7$

$49 != x_0$

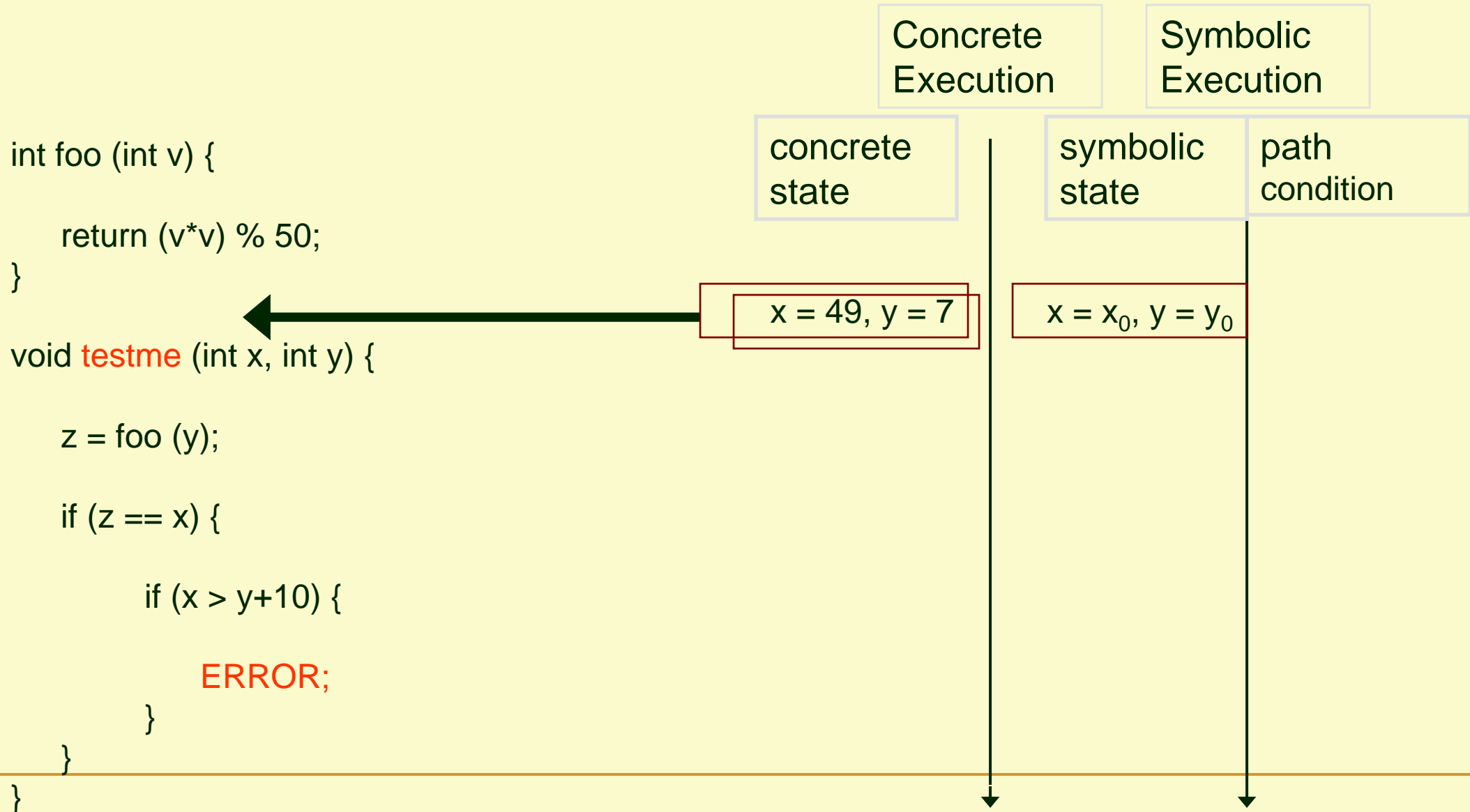
$x = 22, y = 7,$   
 $z = 48$

$x = x_0, y = y_0,$   
 $z = 49$

**ERROR;**



# Example : Simultaneous Concrete and Symbolic Execution



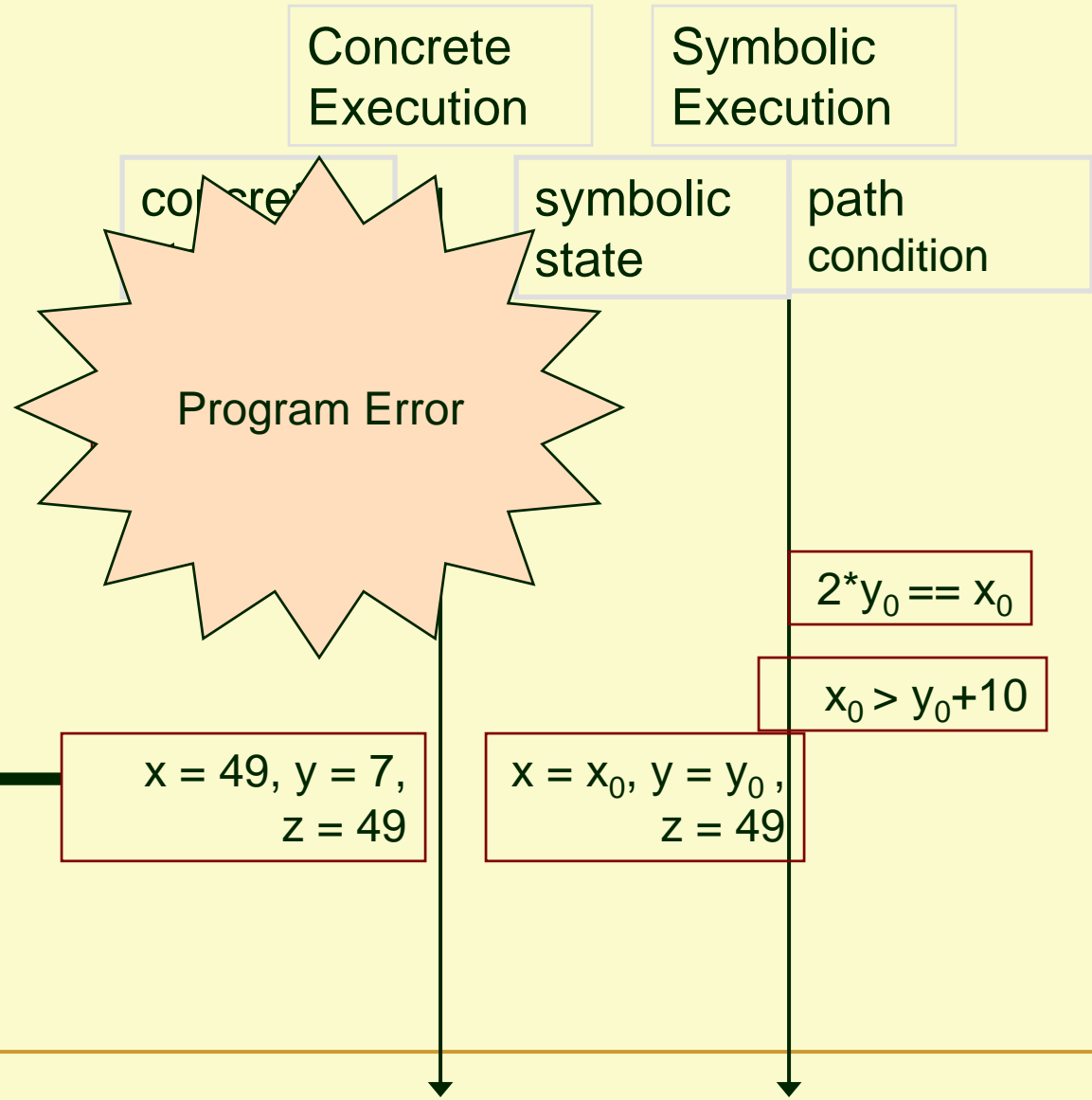
# Example : Simultaneous Concrete and Symbolic Execution

```

int foo (int v) {
    return (v*v) % 50;
}

void testme (int x, int y) {
    z = foo (y);
    if (z == x) {
        if (x > y+10) {
            ERROR;
        }
    }
}

```



# Concolic Testing in a Nutshell

- Use Concolic Execution to Generate
  - Data input

- Use generated data input to
  - Execute program both concretely and symbolically (concolically)

- Use concrete execution to Guide symbolic execution
  - Use smart search strategies: e.g. *Concolic Walk* in space defined by constraints

- Use symbolic execution to
  - To generate data input

# Concolic Execution for Concurrent Programs

- Schedules are another branching condition
- Partial order reduction helps
  - Multistep Semantics for Actors
- Still too many interleavings..
  - Use backward symbolic execution
  - Branch coverage is an uninteresting metric
- Unchecked conditions
  - Runtime Verification

# Decentralized Runtime Verification

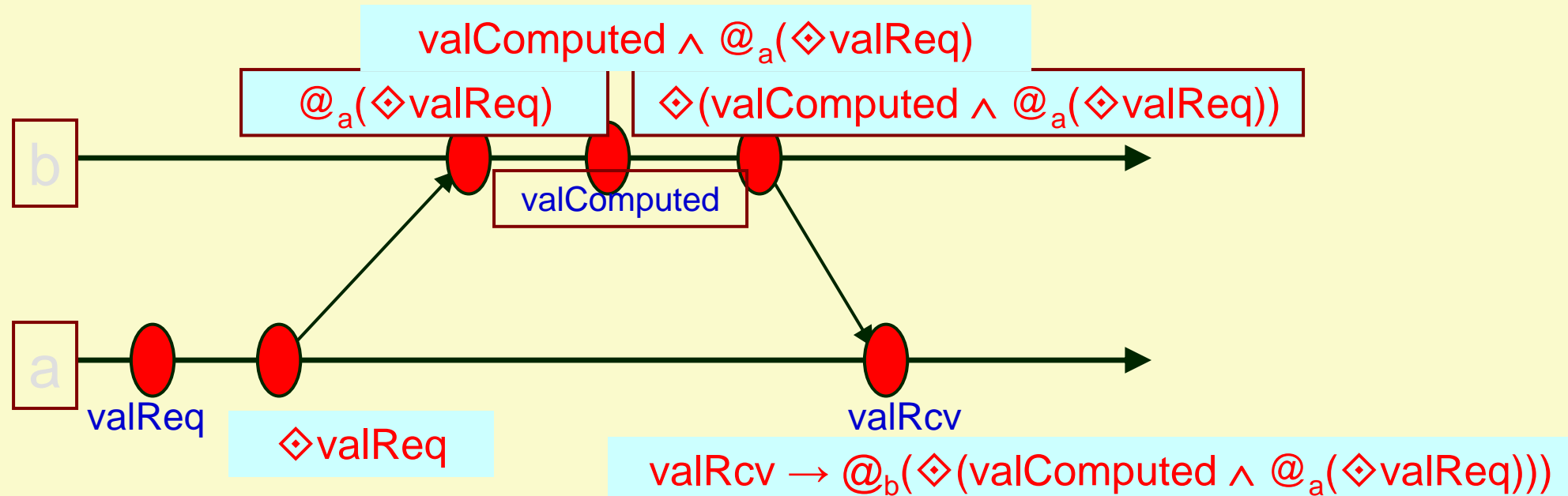
- Properties expressed with respect to an actor (Epistemic Logic)
- Properties are in Distributed Temporal Logic
- Decentralize Monitoring
  - Maintain knowledge of relevant state at each process
  - Update knowledge with incoming messages
  - Attach knowledge with outgoing messages
  - At each actor check safety property against local knowledge



# Decentralized Monitoring Example

“If **a** receives a value from **b** then **b** calculated the value after receiving request from **a**”

$$\text{valRcv} \rightarrow @_b(\diamond(\text{valComputed} \wedge @_a(\diamond \text{valReq})))$$

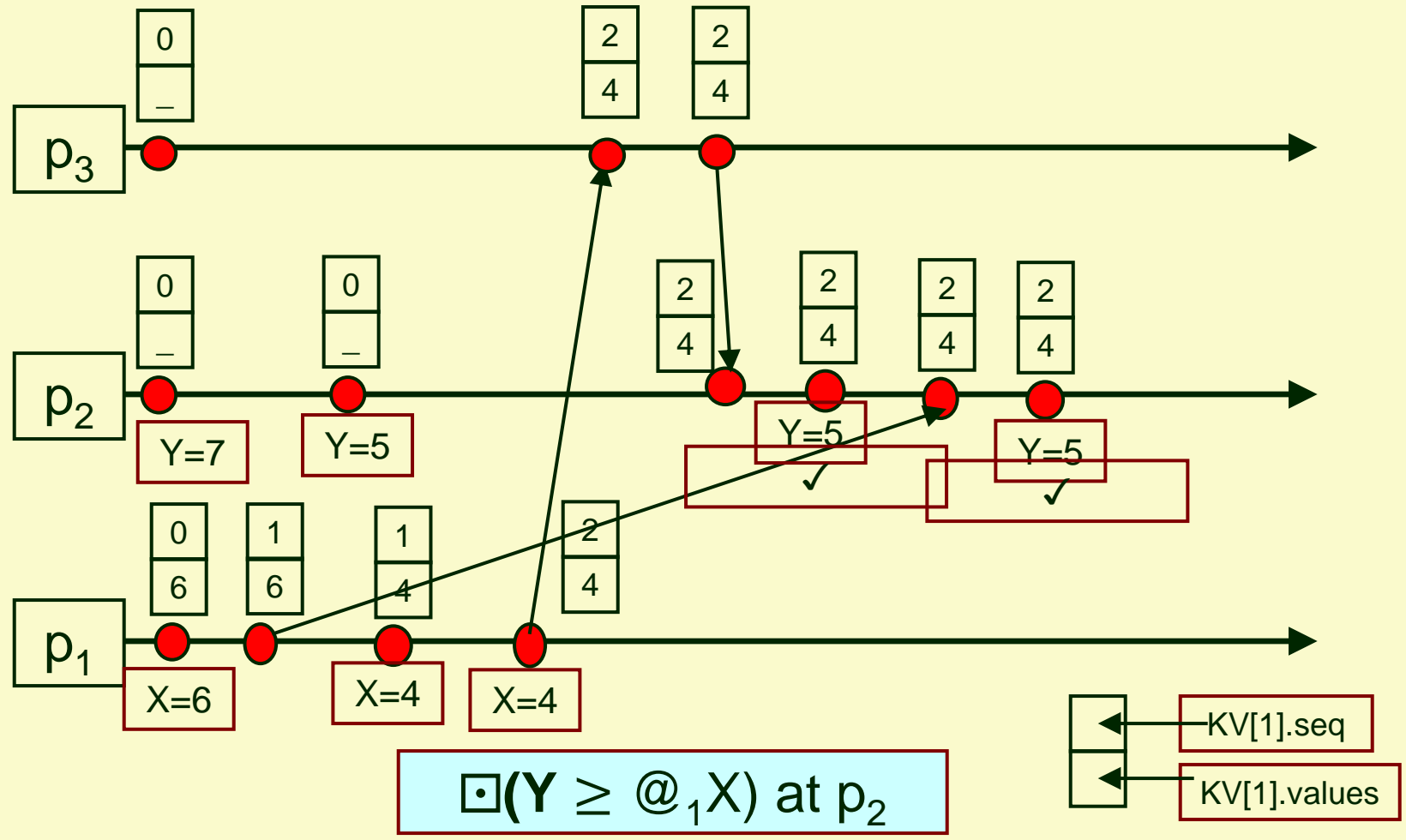


# Knowledge Vector

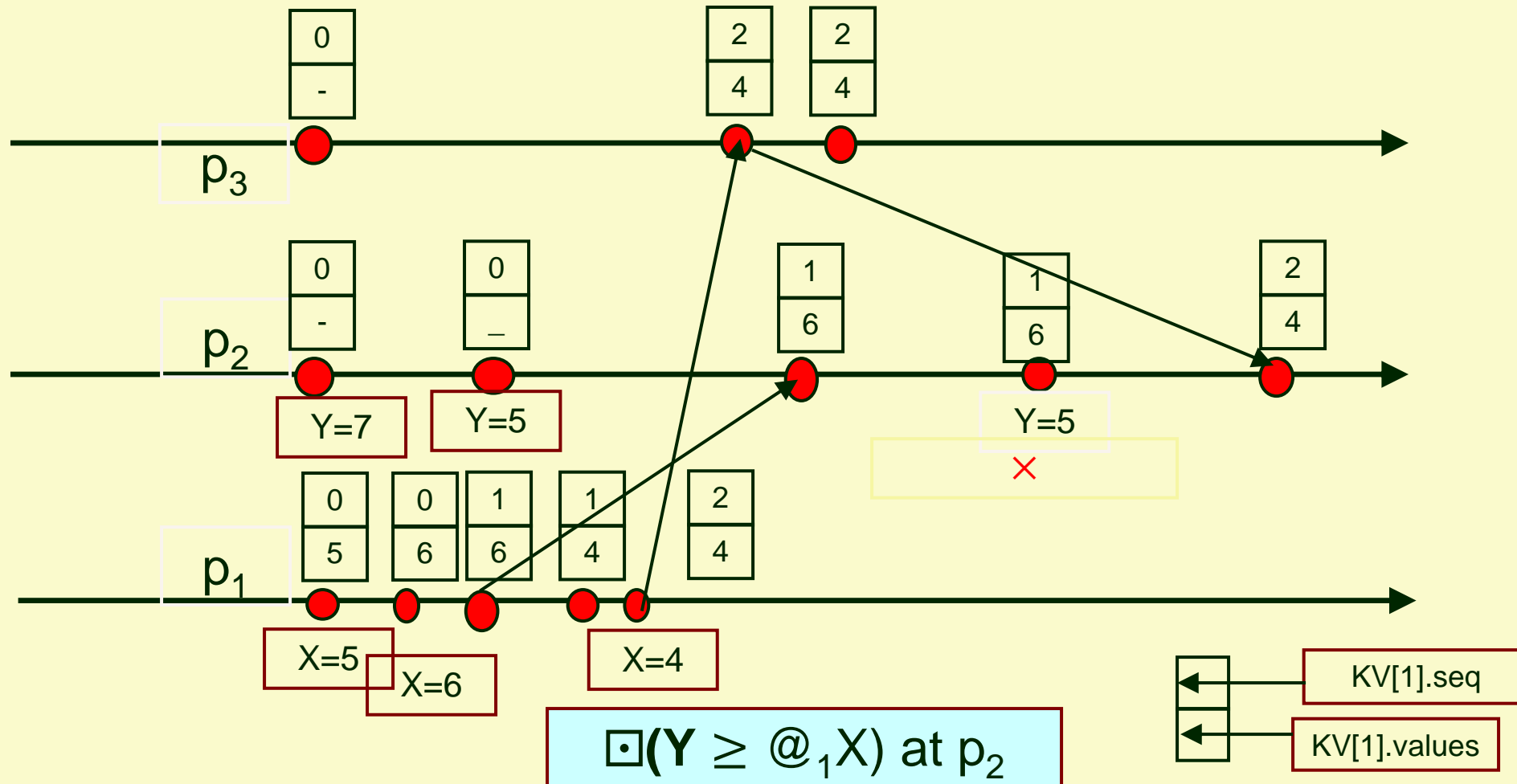
Let  $KV$  be a vector.  $KV$  is a knowledge vector if it has:

- one entry for each process appearing in formula
- $KV[j]$  denotes entry for actor  $j$
- $KV[j].seq$  is the sequence number of last event seen at actor  $j$
- $KV[j].values$  stores values of  $j$ -expressions and  $j$ -formulae

# Example



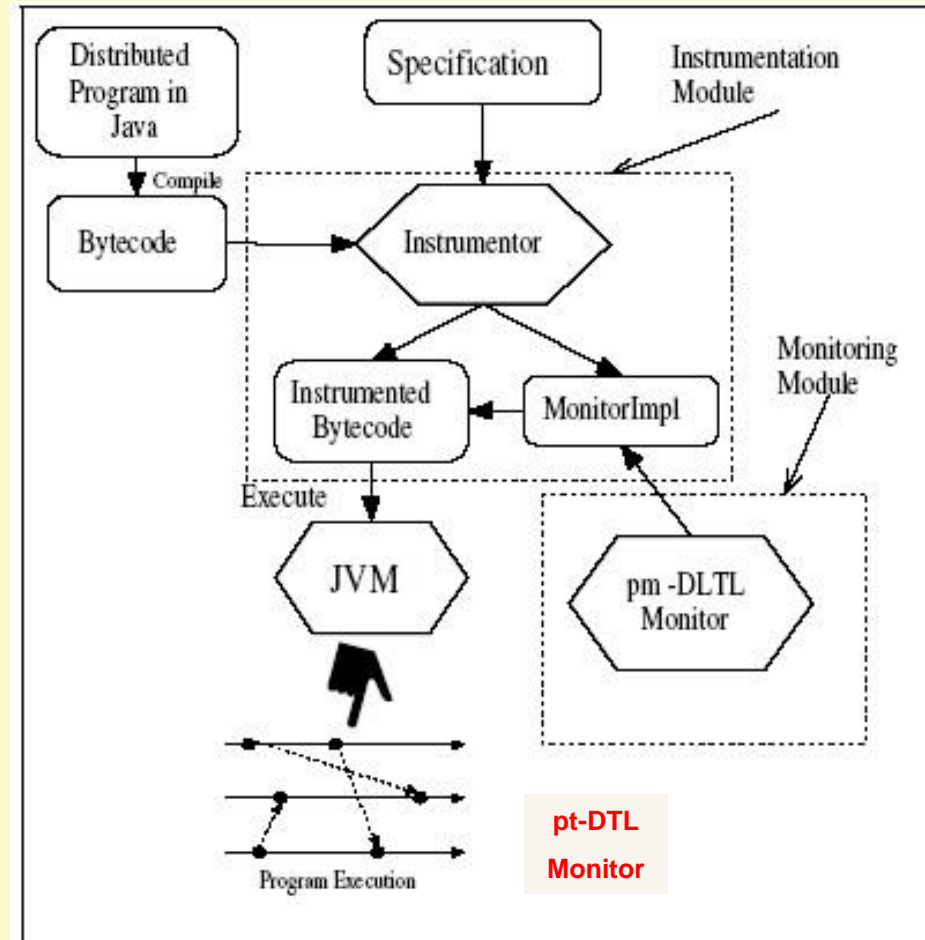
# Example: Another Potential Execution



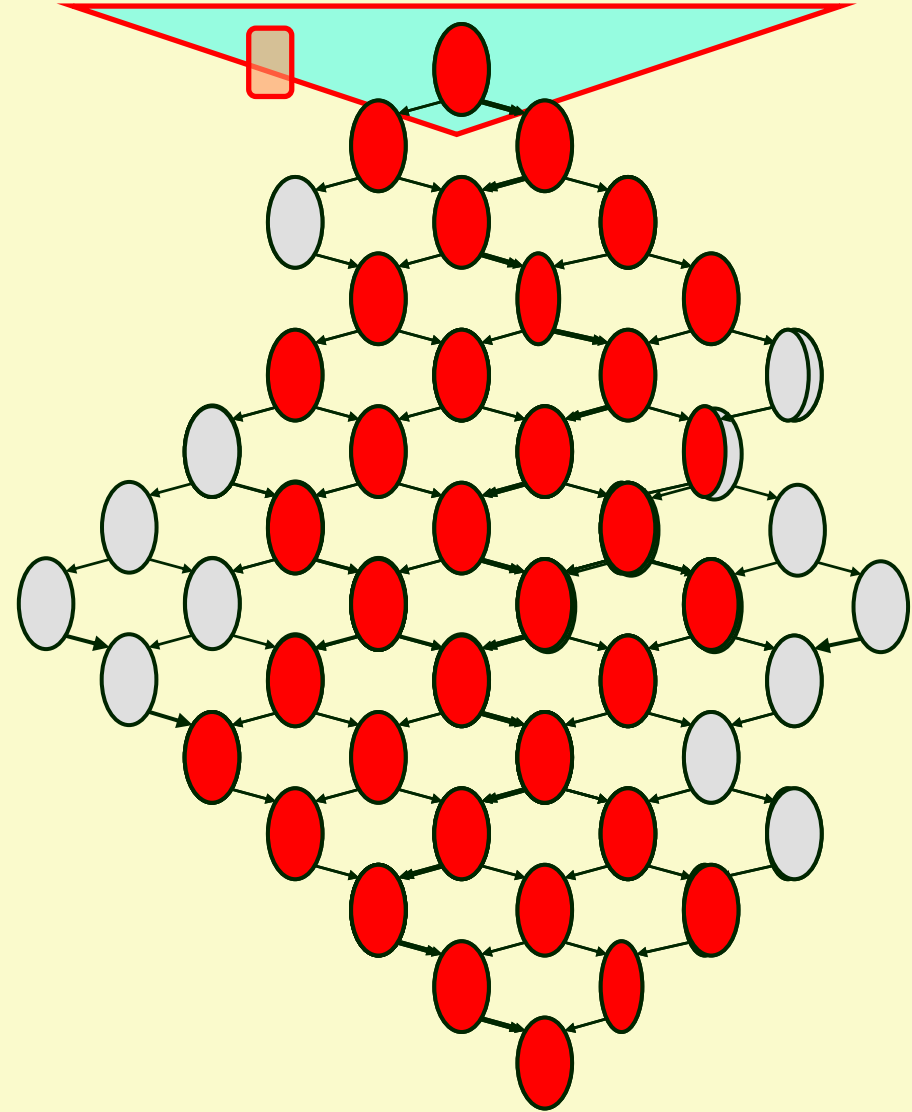
# Predictive Monitoring

- Can predict the violation from the run that did not have the violation.
- Cannot detect a violation if there is no direct communication of intermediate value from p1 to p2

# DIANA Architecture

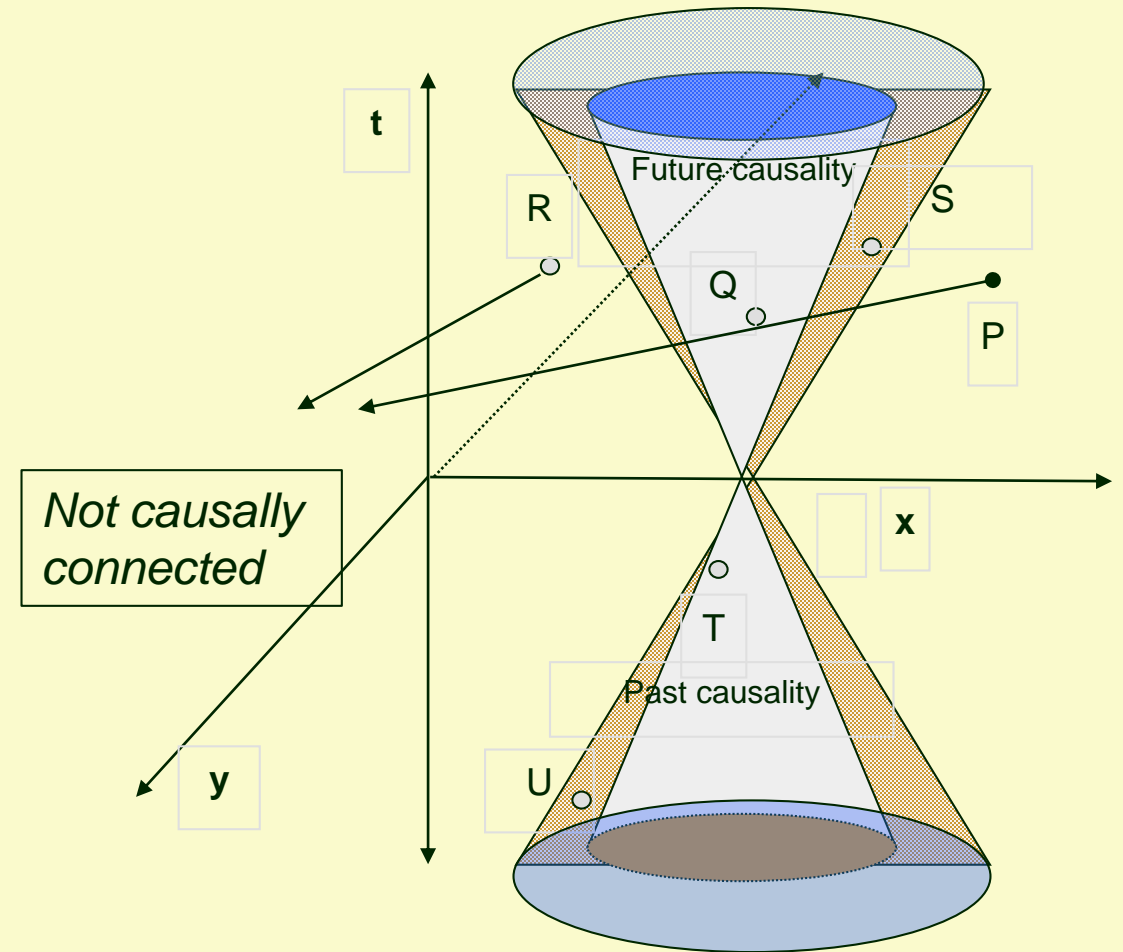


# Causality Cone Heuristics



# Probabilistic Programs

- An actor program is a probabilistic program in a distributed space with concurrent time.
- The behavior of a program is statistical in nature.





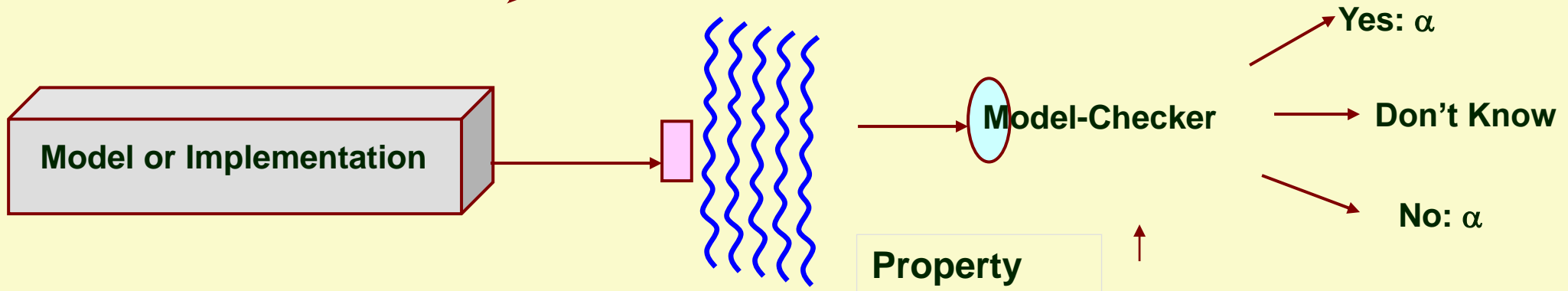
# Properties in CSL sub-logic

- $\phi ::= \text{true} \mid a \mid \phi \wedge \phi \mid : \phi \mid P_{Q p}(\psi)$
- $\psi ::= \phi \text{ U}^{<t} \phi \mid X \phi$   
where  $Q \in \{<, >, \cdot, \cdot\}$
- $P_{<0.5}(\diamond^{<10} \text{full})$ 
  - Probability that queue becomes full in 10 units of time is less than 0.5
- $P_{>0.98}(: \text{retransmit U}^{<200} \text{receive})$ 
  - Probability that a message is received successfully within 200 time units without any need for retransmission is greater than 0.98

# Statistical Model Checking

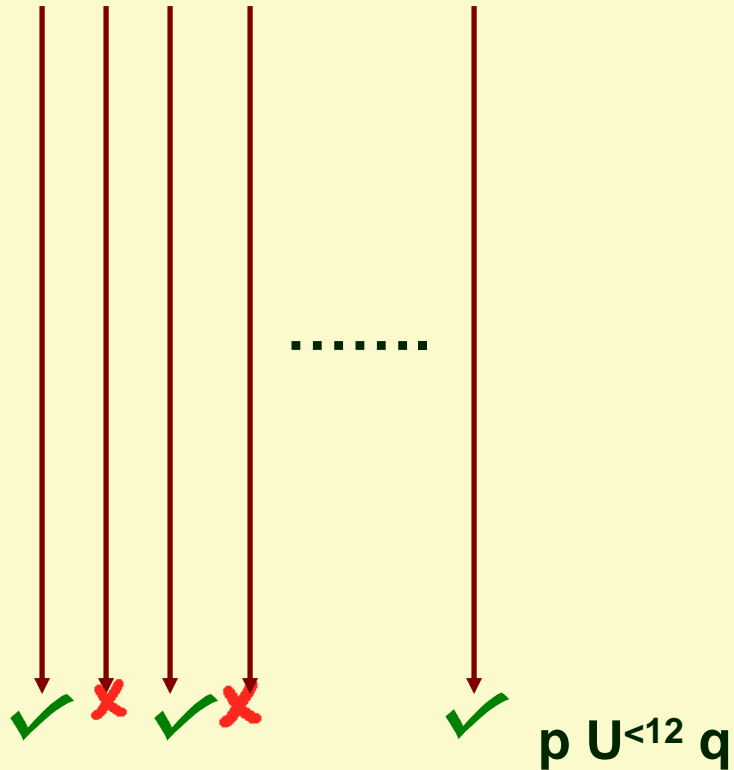


- Decoupled from the tool
  - Run implementation to generate samples, or
  - Get Samples from Monte-Carlo simulation of model



# Checking $P_{<0.6}(p \cup^{<12} q)$ statistically at $s$

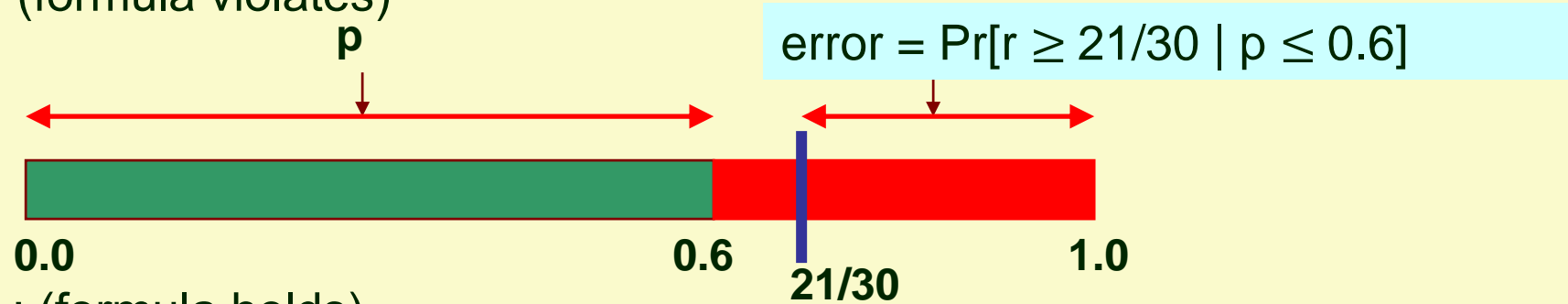
Sample contains, say, 30 paths from  $s$



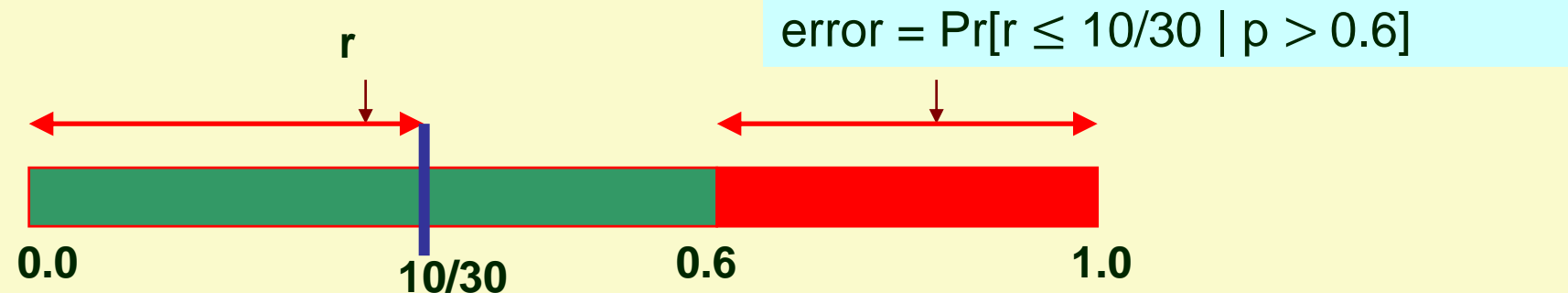
- On 21 paths  $(p \cup^{<12} q)$  is satisfied
- $21/30 > 0.6$ 
  - can we say that  $P_{<0.6}(p \cup^{<12} q)$  is violated at  $s$  ??
  - Statistically, yes, provided we quantify the error in our decision
- **error** =  $\alpha$
- = **Pr**[On 21 (or more) out of 30 paths  $(p \cup^{<12} q)$  hold  
| probability that  $(p \cup^{<12} q)$  holds on a path is less  
than 0.6]
- **Pr**[ $X \geq 21$ ] where  $X \sim \text{Binomial}(30, 0.6)$

# Error (p-value)

- Let  $r = (\# \text{ of paths on which } (p \cup^{<12} q) \text{ hold} / \# \text{ of total paths})$
- Let  $p = \Pr[(p \cup^{<12} q) \text{ holds on a path}]$
- “no” answer : (formula violates)



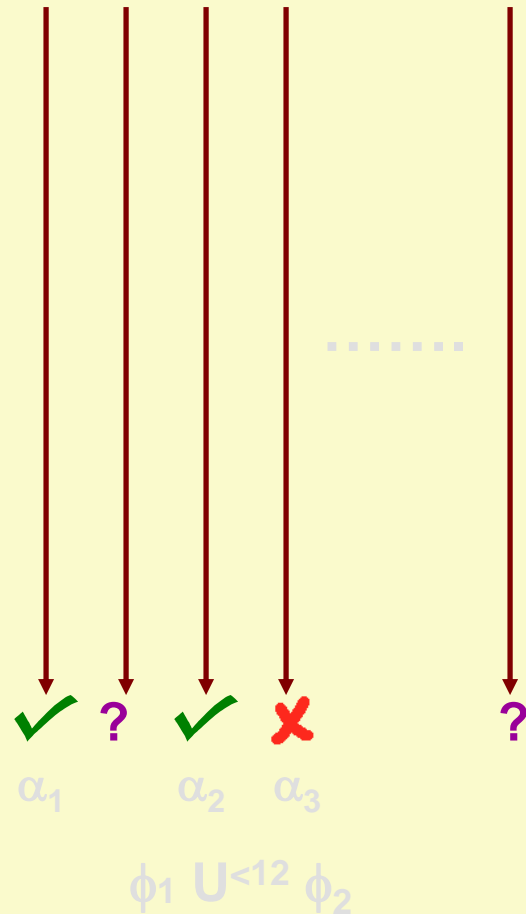
- “yes” answer : (formula holds)



## Nested: Checking $P_{<0.6}(\phi_1 U^{<12} \phi_2)$ at $s$

- $\phi_1$  and  $\phi_2$  contain nested probabilistic operators
- Checking  $(\phi_1 U^{<12} \phi_2)$  over a path
  - Answers are **not** simply “yes” or “no”
  - Answers can be
    - “yes” with error  $\alpha$
    - “no” with error  $\alpha$
    - “don’t know”
- Need a modified decision procedure
  - Handle “don’t know” to get useful answers
  - Incorporate error of decision for sub-formulas

# Checking $P_{<0.6}(\phi_1 U^{<12} \phi_2)$ at $s$ (Problem)

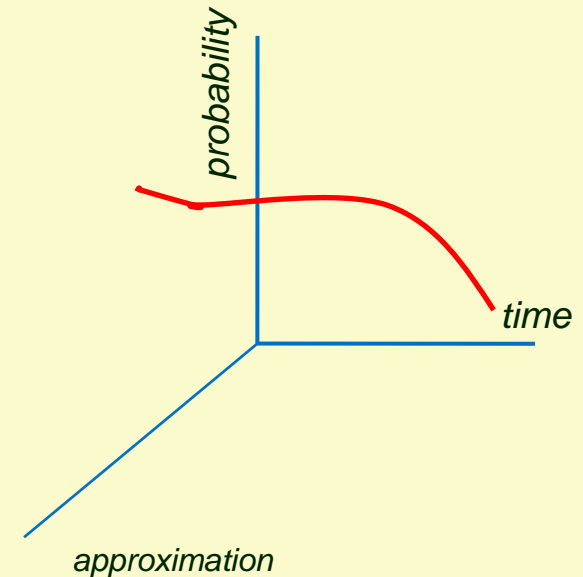


## Solution

1. Resolve “don’t know” (?) in **adversarial** fashion
  - **Observation region**
2. Create “**uncertainty region**” to incorporate error associated with sub-formulas.

# Evolving Systems

- *Big data applications require approximate answers in a real-time.*
- *Probabilistic actor-based programming*
- *Adaptive programs:*
  - *Use predictive distributed monitoring and statistical inference.*
  - *Learning and prediction using Bayesian methods*



# Representing State

- 100 nodes, 5 Abstract States  $\rightarrow 5^{100}$  potential states
- Interested in aggregate properties or expected values
- Model state as pmf vector (superposition of probabilities)

$$s = \begin{array}{|c|c|c|c|c|} \hline s_1 & s_2 & s_3 & \dots & s_n \\ \hline \end{array}$$

$$s = p_1 s_1 + p_2 s_2 + \dots + p_n s_n$$



# Evolution of Probability Distributions

- Transitions may be governed by a Markov model
- pmf vector defines the initial state for a DTMC
  - Search in an *Euclidean space*
  - Property stabilizes after a computable depth
- Model checking reduced to linear algebra
- *Euclidean Model Checking*

# Conclusions

- Programming based on the Actor Model facilitates scalable, secure development of concurrent programs.
  - Probabilistic programming methods needed
- New reasoning methods needed:
  - Scalable
  - Model probabilistic computation
  - Address quantitative properties

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